



NO_x photocatalytic degradation employing concrete pavement containing titanium dioxide

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ABSTRACT

In the present work the degradation of nitrogen oxides (NO_x) by concrete paving stones containing TiO₂ to be applied in road construction is studied. A kinetic model is proposed to describe the photocatalytic reaction of NO_x (combining the degradation of NO and the appearance and disappearance of NO₂) in a standard laminar flow photoreactor irradiated with UV lamps employing only NO as the contaminant source. In addition, the influences of several parameters that can affect the performance of these stones are investigated, such as NO inlet concentration, reactor height and flow rate. The kinetic parameters present in the NO and NO₂ reaction rate are estimated employing experimental data obtained in the photoreactor. The obtained model predictions employing the determined kinetic constants are in good agreement with the experimental results of NO and NO₂ concentration at the reactor outlet.

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1. Introduction

Heterogeneous photocatalysis represents an emerging environmental control option for the efficient removal of chemical pollutants and it can be applied to water and air purification. This process involves a nano-solid semiconductor catalyst, regularly titanium dioxide (TiO₂), which is activated with ultraviolet light of the appropriate wavelength. For various reasons repetitively reported, titanium dioxide in the form of anatase has been the preferred choice due to its strong oxidizing power under UV irradiation, its chemical stability and the absence of toxicity [1]. These reactions are very attractive for treating pollution problems because: (1) in the vast majority of the cases transform pollutants into innocuous products [2–4] and (2) have very low selectivity, thus permitting the treatment of a wide range of contaminants.

Nitrogen oxides (NO_x) are the generic term for a group of highly reactive gases, most of them emitted in air in the form of nitric oxide (NO) and nitrogen dioxide (NO₂). Nitrogen oxides are for instance formed when fuel is burned at high temperatures, as it is the case in combustion processes in automobiles. NO_x causes a wide variety of health and environmental impacts, like the formation of tropospheric ozone and urban smog through

photochemical reactions with hydrocarbons. Furthermore, NO_x together with SO_x (sulfur dioxide and sulfur trioxide) is the major contributor to the “acid rain”, one of the most serious environmental problems across the world. Thus, NO_x emission is a focus of environmental regulations, especially in the ozone non-attainment areas.

The European Union (EU) has taken important steps over the past decade leading to a decrease in the emissions to air and water of a number of pollutants. One of its directives (1999/30/EC) [5] establishes limit values for concentrations of sulfur dioxide, nitrogen dioxide and oxides of nitrogen, particulate matter and lead in ambient air. Some of the pollutant emissions have since become more or less manageable; however particulates, NO_x and smog are still problematic.

To date, a number of researchers have investigated the dynamics of the photocatalysis of nitrogen oxides. While some of the NO_x control methodology is to reduce NO_x back to N₂ [6], another approach is to oxidize NO to NO₂ and HNO₃ along the general direction of nitrogen fixation. Photocatalytic oxidation (PCO) of NO_x offers the following distinctive advantages: (1) no extra reactants required and (2) NO_x recycled or recovered as nitric acid, a potential raw material for fertilizers. In 1994, Japanese researchers reported the photodegradation of NO_x in the ambient atmosphere, using TiO₂ as the photocatalyst [7]. Hashimoto et al. [8] reported the photocatalytic reaction of NO with TiO₂ and zeolite to remove NO_x in the atmosphere. Dalton et al. [9] investigated the NO_x adsorbate reaction at the TiO₂ substrate surface. Ichiura et al. [10] studied the photocatalytic oxidation of nitrogen oxides over

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Nomenclature

a_v	active area per unit reactor volume [$\text{dm}^2 \text{dm}^{-3}$]
A	area [dm^2]
B	reactor width [dm]
C	molar concentration [mol dm^{-3}]
D_h	hydraulic diameter [dm]
E	radiative flux [W m^{-2}]
H	reactor height [dm]
k	reaction rate constant [$\text{mol dm}^{-2} \text{min}^{-1}$]
K	adsorption equilibrium constant [$\text{dm}^3 \text{mol}^{-1}$]
L	reactor length [dm]
L_d	length for a fully developed parabolic velocity profile [dm]
N	number
Q	flow rate [l min^{-1}]
r	superficial reaction rate [$\text{mg dm}^{-2} \text{min}^{-1}$]
Re	Reynolds number
t	time [min]
v	velocity [dm min^{-1}]
V	volume [dm^3]
x	Cartesian coordinate [dm]

Greeks letters

η	dynamic viscosity [$\text{g m}^{-1} \text{s}^{-1}$]
ρ	density [g m^{-3}]
ν	kinematic viscosity [$\text{m}^2 \text{s}^{-1}$]

Subscripts

act	active
ads	adsorbed
air	air
in	inlet condition
NO	nitric oxide
NO ₂	nitrogen dioxide
out	outlet condition
reactor	reactor

titanium dioxide sheets containing metal compounds. In addition, Devahasdin et al. [11] studied the transient behavior and reaction kinetics of the NO photocatalytic degradation, and discussed the feasibility of nitrogen fixation in the flue gas treatment with photocatalytic oxidation. Lin et al. [12] examined the photocatalytic degradation of nitrogen oxides over titania-based photocatalyst illuminated by ultraviolet and visible light. Shelimov et al. [13] analyzed the efficiency of TiO₂ dispersed over alumina support in the photocatalytic removal of NO_x.

The development of innovative materials that can be easily applied on structures, with both de-soiling and de-polluting properties, is a significant step towards improvements of air quality. The use of TiO₂ photocatalyst in combination with cementitious and other construction materials has shown a favorable effect in the removal of air pollutants [14]. In recent years, a wide number of laboratory scale tests have been performed, under different experimental conditions, in order to evaluate the NO_x degradation properties of TiO₂ photocatalytic materials [15–20]. The application of photocatalytic materials is protected by several patents [21–25].

However, few of the studies mentioned above have considered the reaction kinetics of the NO and NO₂ together as a series-parallel

or consecutive-competitive reaction and none of them have proposed a kinetic expression for the appearance–disappearance of NO₂. Only reaction rate expressions for the degradation of NO were proposed, which sometime involve the effect of the NO₂ concentration. For instance, Devahasdin et al. [11] proposed a NO reaction rate equation in function of the NO₂ concentration. On the other hand, Hashimoto et al. [8] performed an active site balance for NO and NO₂ and proposed two expressions corresponding with the equilibrium adsorption concentrations for both species.

In the present work, the degradation of NO_x compounds employing commercial concrete paving stones with TiO₂ to be applied in road construction is studied experimentally and theoretically. The experiments were carried out in a photoreactor designed according to standard ISO 22197-1 [26] to assess these kinds of photocatalytic materials employing NO as the pollutant source. Furthermore, a kinetic model is proposed to describe the photocatalytic oxidation of NO_x (NO and NO₂). A reaction rate expression for the oxidation of NO as well as for the appearance and disappearance of NO₂ are postulated and the kinetic parameters are determined employing the experimental data. In addition, the influence of several parameters that can affect the performance of these stones, such as NO inlet concentration, reactor height and flow rate is studied. The relative humidity, temperature and irradiance were kept constant during this study. Finally, the model predictions with the estimated kinetic constants are compared with the experimental results yielding a good agreement between them.

2. Experimental setup and measurements

The standard ISO 22197-1 [26] serves as a sound basis for measurements, its recommendations were largely followed for the practical conduction of the present study. In fact, this standard holds for advanced technical fine ceramics but it satisfies the needs for measurements on concrete specimen as well.

The applied apparatus is composed of a reactor cell housing the sample, a suitable light source, a NO_x analyzer, and an appropriate gas supply (Fig. 1).

2.1. Reactor

The core of the experimental setup is a gas reactor allowing a planar sample of the size 100 mm × 200 mm to be embedded. The schematic representation of the gas reactor is given in Fig. 2.

Furthermore, the reactor is made from materials which are non-adsorbing to the applied gas and can withstand UV light of high radiation intensity. On top the reactor is tightly closed with a glass pane made from borosilicate, allowing the UV-radiation to pass through with almost no resistance. Within the reactor the planar surface of the specimen is fixed parallel to the covering glass, leaving an alterable slit height H (most commonly 3 mm) for the gas to pass through. The active sample area used for degradation was, deviating from the standard, enlarged from 49.5 mm ± 0.5 mm in width and 99.5 mm ± 0.5 mm in length to $B = 100$ mm and $L = 200$ mm (with similar tolerance), which better complies with standard paving stone dimensions. By means of profiles and seals, the sample gas only passes the reactor through the slit between sample surface in longitudinal direction and the glass cover. All structural parts inside the box are designed to enable laminar flow of the gas along the sample surface and to prevent turbulences.

2.2. Light source

The applied light source is composed of three fluorescent tubes (Philips CLEO Compact) of each 25 W, emitting a high-concentrat-

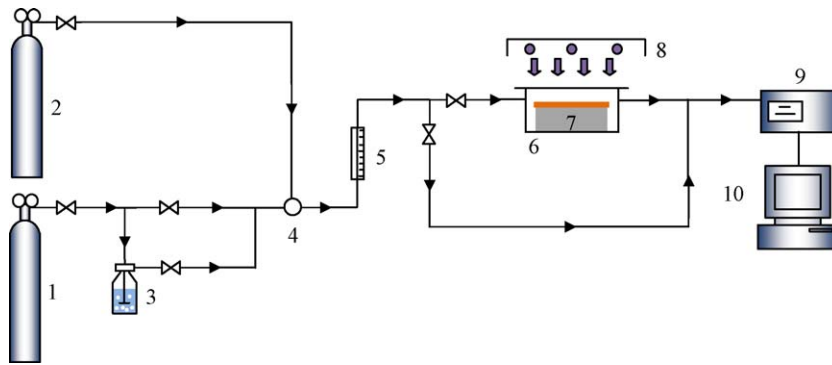


Fig. 1. Schematic representation of the experimental setup. (1) Synthetic air. (2) NO source. (3) Gas-washing bottle. (4) Temperature and relative humidity sensor. (5) Flow controller. (6) Gas photoreactor. (7) Paving stone sample. (8) Light source. (9) NO_x analyzer. (10) Computer.

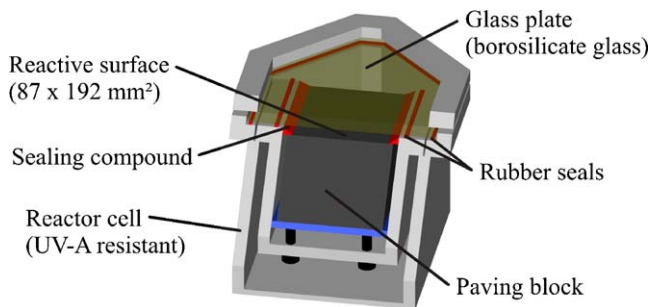


Fig. 2. Schematic diagram of the gas photoreactor.

ed UV-A radiation in the range of 300–400 nm with maximum intensity at about 345 nm (Fig. 3). Due to the narrow range in wavelength, an addition of a filter was not necessary. A warming of the reactor by the light source is not expected due to the spatial separation of light source and reactor, and a cooling of the lamp by means of fans. All fluorescent tubes can be adjusted in irradiance. With the help of a calibrated UV-A radiometer the irradiance is adjusted to 10 W m^{-2} at the sample surface. A lead time of about 15 min has to be considered for fluorescent tubes till a stable UV-A radiation is approached. The UV-A irradiance profile within the test setup and surrounding the reactor box can be observed in Fig. 4.

2.3. Testing gas supply and gas types

For the conduction of the experiment, two different types of gas, filled in standard gas cylinders, are necessary. First, the model contaminant is discussed. For the pollution of the sample surfaces,

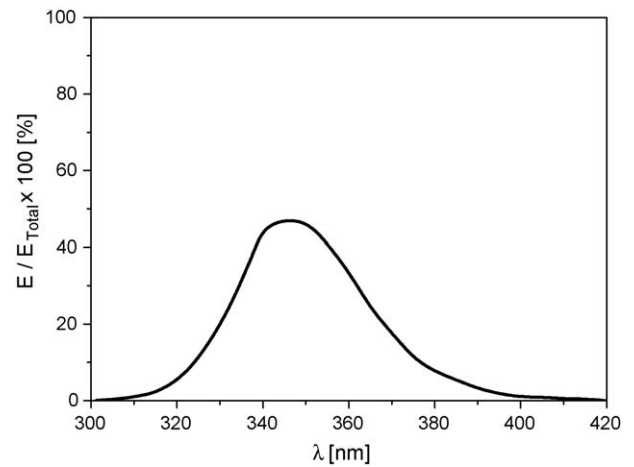


Fig. 3. Spectral distribution of the relative emission of the employed lamps.

nitric oxide (NO) is employed. The used gas is composed of 50 ppmv NO which is stabilized in nitrogen (N₂). As the concentration of gas, finally applied to the sample, is adjusted to 1 ppmv, only small quantities of this gas are required. As transport fluid synthetic air, being composed of 20.5 vol.% of oxygen (O₂) and 79.5 vol.% of nitrogen, is used.

Since the gas cylinders are under high pressure, the gas needs to pass a pressure reducing valve before entering the system. Here, pressure is first reduced to 0.3 bar. Before the two gas flows are merged, the model contaminant has to pass a high precision valve in order to adjust a pollution of 1 ppmv NO to the sample. The NO concentration can be monitored with the NO analyzer, connected

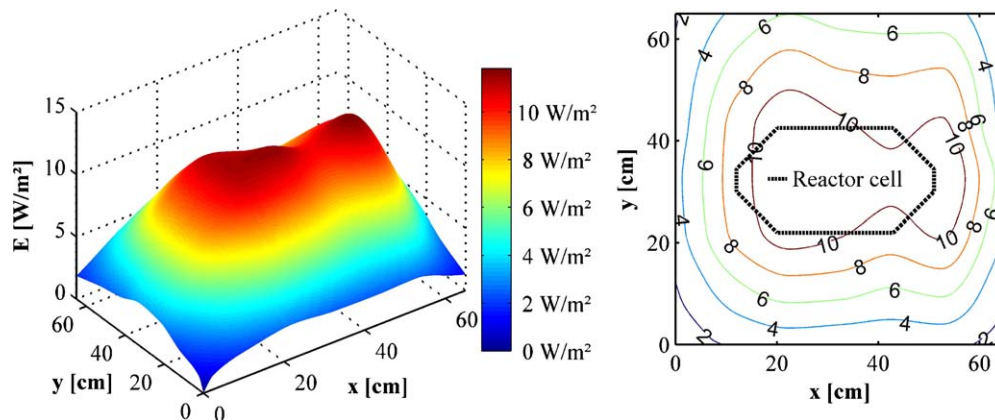


Fig. 4. Distribution of UV-A irradiance within the test setup (left) and placement of the reactor box (right).

to the outlet of the reactor box. Furthermore, the synthetic air is conveyed through a gas-washing bottle, filled with demineralized water, in order to keep the relative humidity of the supplied gas constant at 50%. Using a split gas flow, with one line passing a valve before the gas-washing bottle, the desired humidity can be adjusted. Behind these two stages both gas flows, polluted and transport fluid, are mixed. With the help of a flow controller a volume flow of $Q = 3 \text{ l min}^{-1}$ is adjusted. The Reynolds number of the flow reads:

$$Re = \frac{v_{\text{air}} D_h \rho_{\text{air}}}{\eta_{\text{air}}} = \frac{2v_{\text{air}} H \rho_{\text{air}}}{\eta_{\text{air}}} = \frac{2Q}{B v_{\text{air}}} \quad (1)$$

D_h is the hydraulic diameter of the considered channel, defined as four times the cross-sectional area divided by the perimeter, for the slit considered here, $D_h = 2H$. Substituting $Q = 3 \text{ l min}^{-1}$, $B = 100 \text{ mm}$ and $v_{\text{air}} = 1.54 \times 10^{-5} \text{ m}^2 \text{ s}^{-1}$ (1 bar, 20°C) yields $Re \approx 65$. Considering $H = 3 \text{ mm}$, the mean air velocity v_{air} is 0.17 m s^{-1} along the sample surface.

This low Reynolds number implies that the flow is laminar. A fully developed parabolic velocity profile will be developed at $L_d = 0.05 Re 2H$, so here $L_d \approx 20 \text{ mm}$, i.e. only at the first 10% of the slit length there are entrance effects, during the remaining 90% there is a fully developed laminar flow profile.

The gas, mixed and humidified this way, enters the reactor and is conveyed along the illuminated sample surface. At the opposite site of the reactor the gas leaves the chamber and is transported to a flue or outside with the help of an exhaust air duct. The NO_x analyzer samples the reacted gas from this exhaust line. An adequate dimensioning of the hose line and, possibly, the installation of non-return valves prevents from suction of leak air from outside via the hose line to the analyzer.

2.4. Analyzer

For the gas analysis a chemiluminescent NO_x analyzer is employed. The analyzer measures the NO_x and NO concentration in steps of 5 s while the corresponding NO_2 concentration is computed by the difference of the previous two. During the measurement the analyzer is constantly sampling gas with a rate of 0.8 l min^{-1} . The detection limit of the employed analyzer is at about 0.5 ppbv.

2.5. The conduction of measurements

For the development of a reaction model and the herewith related experiments one sample, a paving stone, was used. This way differences in measurement results due to varying surface roughness or unequal distribution of catalyst can be neglected. The employed sample is a commercially available concrete paving stone whose photocatalytic properties were tested beforehand [27] and is a double layer stone with the upper layer being photocatalytically active. This upper layer was prepared mixing dry powders of normal concrete with TiO_2 powder before adding water to the mixture. Further information about the concrete recipe cannot be provided because it is confidential information of the manufacturing company.

In preparation of each measurement the sample surface is cleaned with demineralized water in order to remove fouling, contamination and potential reaction products due to a previous NO_x degradation. Subsequently, the sample is dried in a drying oven for 24 h. For the measurement, the sample is placed in the reaction chamber and with the help of an elastic sealing compound all gaps and joints are sealed that way that the fed air can only pass the reactor along the reactive sample surface. A metal sheet of the dimension $87 \text{ mm} \times 192 \text{ mm}$ is employed as a template for the

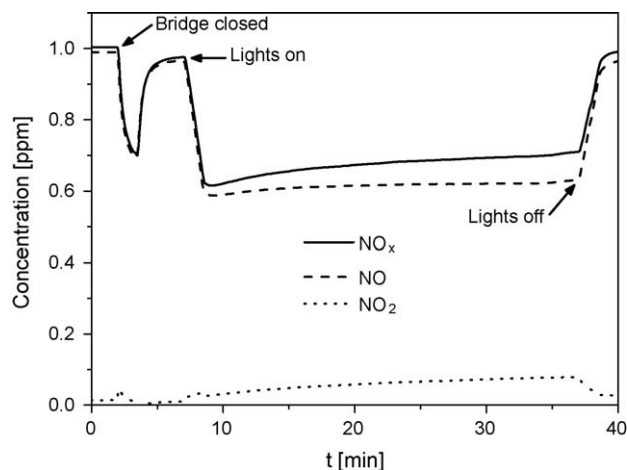


Fig. 5. Representative experimental result. $H = 3 \text{ mm}$. $Q = 3 \text{ l min}^{-1}$. $C_{\text{NO}_x, \text{in}} = 1.0 \text{ ppm}$. 50% relative humidity. $E = 10 \text{ W m}^{-2}$.

sealing. Therefore, the active sample surface is kept exactly identical for all measurements.

After assembling the sample the reactor is closed and the gas supply is started. The UV-A source is switched on as well in order to start the radiation stabilization, but the reactor stays covered to prevent first degradation. With the help of the controls the flow and relative humidity are now adjusted. The supplied NO concentration is adjusted to the desired inlet concentration, which is checked by the analyzer. When these conditions are stable the bridge is closed and the gas flows along the reactor. During this time the measured NO outlet concentration of the reactor decreases and then approaches again the original inlet concentration. This phenomenon describes the saturation of surface with NO as well as the non contaminated air removal from the reactor and has been found to be a function of flow velocity, inlet concentration and surface character of the sample. After this period of time, the cover sheet is removed to allow the UV-radiation passing through the glass. The degradation for the uncovered reactor lasts for 30 min, then the reactor is covered again and the data acquisition is continued for further 5 min. Within the last minutes of measurement the NO and NO_x concentrations return to the original scale. An example of a representative experiment result is shown in Fig. 5, where the different steps mentioned above can be observed.

In order to obtain sufficient data for the development of a reaction model, varying NO inlet concentrations of 0.1, 0.3, 0.5, and 1.0 ppmv were applied. Furthermore, for each inlet concentration the flow rate was varied by using flows of 3 and 5 l min^{-1} . These different volumetric flows correspond to flow velocities of 0.167 and 0.278 m s^{-1} at the sample surface inside the reactor box. With these combinations a total number of 8 measurements were executed plus 4 repetitions under certain operation conditions (Table 1).

In addition, five more measurements with the above given flow rates but a fixed NO inlet concentration of 0.3 ppmv have been done. In doing so, the slit height in the reactor box was varied (2, 3 and 4 mm) for each flow rate. However, stable and measurable NO inlet concentration could not be achieved while applying a flow of 5 l min^{-1} and using a slit height of only 2 mm and this experiment was excluded.

2.6. Modelling

The photocatalytic oxidation mechanism of NO_x mixture is reported in many publications [7,9,11,13,17]. All of them proposed the NO decomposition to NO_2 , and then NO_2 to NO_3H through the hydroxyl radical attack generated during the photocatalyst

Table 1

Experimental results of the photocatalytic NO degradation with an active concrete surface for different operating conditions.

Experiment #	Q l min ⁻¹	H mm	C _{NO,in} ppm	C _{NO,out} ppm	C _{NO₂,in} ppm	C _{NO₂,out} ppm	NO _x conversion %
1	3	3	0.096	0.030	0.002	0.005	64.29
2	3	3	0.304	0.159	0.003	0.006	46.25
3	3	2	0.301	0.162	0.004	0.009	43.93
4	3	4	0.301	0.158	0.005	0.012	44.44
5	3	3	0.505	0.312	0.004	0.008	37.13
6	3	3	0.505	0.342	0.009	0.010	31.52
7	3	3	0.989	0.624	0.015	0.077	30.18
8	3	3	1.001	0.724	0.018	0.080	21.10
9	3	3	1.009	0.736	0.016	0.042	24.10
10	3	3	1.009	0.763	0.014	0.050	20.53
11	5	3	0.102	0.041	0.002	0.008	52.88
12	5	3	0.300	0.197	0.004	0.012	31.25
13	5	4	0.300	0.208	0.005	0.009	28.85
14	5	3	0.502	0.357	–	–	28.88
15	5	3	0.998	0.777	0.020	0.081	15.72

Table 2

Photocatalytic reaction mechanism of nitrogen oxides.

Reaction step								Constant
Activation	TiO ₂	+	hν	→	h ⁺	+	e ⁻	Φ _λ
Absorption	H ₂ O _{gas}	+	Site	⇌	H ₂ O _{ads}			K _W
	O ₂ _{gas}	+	Site	⇌	O ₂ _{ads}			K _{O₂}
	NO _{gas}	+	Site	⇌	NO _{ads}			K _{NO}
	NO ₂ _{gas}	+	Site	⇌	NO ₂ _{ads}			K _{NO₂}
Hole trapping	H ₂ O _{ads}	+	h ⁺	→	*OH	+	H ⁺	k ₁
Electron trapping	O ₂	+	e ⁻	→	O ₂ ⁻			k ₂
Hydroxyl attack	NO _{ads}	+	*OH	→	HNO ₂			k ₃
	HNO ₂	+	*OH	→	NO ₂ _{ads}	+	H ₂ O	k ₄
	NO ₂ _{ads}	+	*OH	→	HNO ₃			k ₅
Superoxide attack	NO _{ads}	+	O ₂ ⁻	→	NO ₃ ⁻			k ₆
Recombination	h ⁺	+	e ⁻	→	Heat			k ₇

activation stage. However, despite of these mechanisms being self consistent, in some of the reaction schemes additional reaction processes are proposed, like O₂⁻ interaction with NO to yield NO₃⁻ [13]. The scheme postulated in the present work is shown in Table 2 considering the studies mentioned above.

The kinetic expression proposed for the NO degradation reaction rate is the corresponding to the Langmuir–Hinshelwood model [11,17,28] which is widely employed for the photocatalytic degradation of a number of contaminants [29–31]. Nevertheless, only few times the photocatalytic kinetic model includes the reaction dependence with other reactants and/or intermediates concentrations (in this case NO₂) [11]. Moreover, the reaction rate should be expressed as a superficial rate for a gas–solid heterogeneous system [18,19,32–35]. Following this model, applied to a heterogeneous reaction, the Langmuir–Hinshelwood kinetic model for NO disappearance rate and NO₂ appearance/disappearance rate for irreversible reactions, per unit area of active surface and for constants relative humidity and irradiance reads:

$$r_{\text{NO}} = -r_3 - r_6 = -\frac{(k_3 + k_6)K_{\text{NO}}C_{\text{NO}}}{1 + K_{\text{NO}}C_{\text{NO}} + K_{\text{NO}_2}C_{\text{NO}_2}} \quad (2)$$

$$r_{\text{NO}_2} = -r_5 + r_4 = -r_5 + r_3 = -\frac{k_5K_{\text{NO}_2}C_{\text{NO}_2}}{1 + K_{\text{NO}}C_{\text{NO}} + K_{\text{NO}_2}C_{\text{NO}_2}} + \frac{k_3K_{\text{NO}}C_{\text{NO}}}{1 + K_{\text{NO}}C_{\text{NO}} + K_{\text{NO}_2}C_{\text{NO}_2}} \quad (3)$$

where r_3 , r_4 , r_5 and r_6 are the superficial reaction rates (mol dm⁻² min⁻¹) of the corresponding stage as Table 2 shows. C_{NO} and C_{NO_2} are the corresponding molar concentration (mol dm⁻³) of NO and NO₂ (which are related to the NO and

NO₂ concentrations in ppm through the air volume under normal condition of 1 bar and 20 °C). k_3 , k_5 and k_6 are the corresponding reaction rate constants (mol dm⁻² min⁻¹) for NO and NO₂. K_{NO} and K_{NO_2} are the adsorption equilibrium constant (dm³ mol⁻¹) for NO and NO₂ respectively, assuming that these species compete for the same active sites.

Here, the adopted hypothesis in the NO₂ reaction rate expression is $r_4 = r_3$, that corresponds to the kinetic or micro steady state for the NO₂H specie, that was found in very low concentration [11].

In addition, other assumptions can be imposed after doing the parameters optimization as shown in next section. A small value of k_6 (8 order of magnitude smaller than k_3) was obtained employing Eqs. (2) and (3) in the parameters optimization tool. Therefore, a simpler kinetic model (with less kinetic parameters) can be achieved by taking into account the hydroxyl attack as the main NO_x degradation mechanism, i.e. the same as Devahasdin et al. [11] have proposed:

$$r_{\text{NO}} = -r_3 = -\frac{k_3K_{\text{NO}}C_{\text{NO}}}{1 + K_{\text{NO}}C_{\text{NO}} + K_{\text{NO}_2}C_{\text{NO}_2}} \quad (4)$$

$$r_{\text{NO}_2} = -r_5 + r_4 = -r_5 + r_3 = -\frac{k_5K_{\text{NO}_2}C_{\text{NO}_2}}{1 + K_{\text{NO}}C_{\text{NO}} + K_{\text{NO}_2}C_{\text{NO}_2}} + \frac{k_3K_{\text{NO}}C_{\text{NO}}}{1 + K_{\text{NO}}C_{\text{NO}} + K_{\text{NO}_2}C_{\text{NO}_2}} \quad (5)$$

Since Hunger et al. [28] have found that this kind of system employing a photocatalytic concrete stone in a flow reactor is not controlled by the mass transport, a plug flow reactor model can be

assumed for the NO and NO₂ balance equations:

$$v_{\text{air}} \frac{dC_{\text{NO}}}{dx} = a_v r_{\text{NO}} \quad (6)$$

$$v_{\text{air}} \frac{dC_{\text{NO}_2}}{dx} = a_v r_{\text{NO}_2} \quad (7)$$

where a_v is the active surface area per unit reactor volume:

$$a_v = \frac{A_{\text{act}}}{V_{\text{reactor}}} \cong \frac{1}{H} [=] \frac{dm_{\text{act}}^2}{dm_{\text{reactor}}^3} \quad (8)$$

and with the following inlet conditions:

$$C_{\text{NO}}(x=0) = C_{\text{NO},\text{in}} \quad (9)$$

$$C_{\text{NO}_2}(x=0) = C_{\text{NO}_2,\text{in}} \quad (10)$$

Replacing the kinetic equations (Eqs. (4) and (5)) in the corresponding mass balances (Eqs. (6) and (7)):

$$v_{\text{air}} \frac{dC_{\text{NO}}}{dx} = -a_v \frac{k_3 K_{\text{NO}} C_{\text{NO}}}{1 + K_{\text{NO}} C_{\text{NO}} + K_{\text{NO}_2} C_{\text{NO}_2}} \quad (11)$$

$$v_{\text{air}} \frac{dC_{\text{NO}_2}}{dx} = a_v \left(-\frac{k_5 K_{\text{NO}_2} C_{\text{NO}_2}}{1 + K_{\text{NO}} C_{\text{NO}} + K_{\text{NO}_2} C_{\text{NO}_2}} + \frac{k_3 K_{\text{NO}} C_{\text{NO}}}{1 + K_{\text{NO}} C_{\text{NO}} + K_{\text{NO}_2} C_{\text{NO}_2}} \right) \quad (12)$$

In addition to the study performed by Hunger et al. [28], the validity of the above mass balance model was assessed using a 2-Dimensional CFD simulation (Comsol Multiphysics). Even though concentration gradients along the vertical direction of the reactor were found, the outlet concentration predicted by the CFD simulations differs in less than 8% from the 1-dimensional plug flow model. Therefore, the 1D mass balance is a suitable approximation for the current flow reactor, despite of the above mentioned laminar flow regime. The simulation results employing the CFD tool will be presented in a forthcoming paper.

3. Resulting solutions

3.1. Approximate solution

Both obtained differential equations (Eqs. (11) and (12)) are connected and they can be only solved numerically employing for instance the Euler method, which will be described in the next section. However, some approximations can be considered in order to get an analytical solution of the mass balances. By dividing Eq. (12) by Eq. (11), a differential equation of NO₂ concentration in function of NO concentration is obtained:

$$\frac{dC_{\text{NO}_2}}{dC_{\text{NO}}} = \frac{k_5 K_{\text{NO}_2} C_{\text{NO}_2}}{k_3 K_{\text{NO}} C_{\text{NO}}} - 1 \quad (13)$$

With the following boundary condition:

$$C_{\text{NO}_2}(C_{\text{NO}} = C_{\text{NO},\text{in}}) = C_{\text{NO}_2,\text{in}} \quad (14)$$

If $k_5 K_{\text{NO}_2} \neq k_3 K_{\text{NO}}$, the solution is:

$$C_{\text{NO}_2} = \left(\frac{C_{\text{NO},\text{in}}}{1 - (k_5 K_{\text{NO}_2} / k_3 K_{\text{NO}})} + C_{\text{NO}_2,\text{in}} \right) \times \left(\frac{C_{\text{NO}}}{C_{\text{NO},\text{in}}} \right)^{k_5 K_{\text{NO}_2} / k_3 K_{\text{NO}}} - \frac{C_{\text{NO}}}{1 - (k_5 K_{\text{NO}_2} / k_3 K_{\text{NO}})} \quad (15)$$

Considering that $C_{\text{NO},\text{in}}/C_{\text{NO}}(x > 0) > 1$, this expression can be simplified if $(k_5 K_{\text{NO}_2} / k_3 K_{\text{NO}}) > 1$ and if $C_{\text{NO}_2,\text{in}} \approx 0$, obtaining:

$$C_{\text{NO}_2} = \frac{C_{\text{NO}}}{(k_5 K'_{\text{NO}_2} / k_3 K'_{\text{NO}}) - 1} \quad (16)$$

where k'_5 , K'_{NO_2} , k'_3 and K'_{NO} denote the kinetic parameters of the approximate model.

In cases where the only fed contaminant is NO, which is the case following the standard ISO 22197-1 [26], $C_{\text{NO}_2}(x=0) = 0$ and $C_{\text{NO}_2} \ll C_{\text{NO}}$ can be assumed [28]. Hence, $1 + K_{\text{NO}} C_{\text{NO}} \gg K_{\text{NO}_2} C_{\text{NO}_2}$ and the NO balance can be written as:

$$v_{\text{air}} \frac{dC_{\text{NO}}}{dx} = -a_v \frac{k'_3 K'_{\text{NO}} C_{\text{NO}}}{1 + K'_{\text{NO}} C_{\text{NO}}} \quad (17)$$

with

$$C_{\text{NO}}(x=0) = C_{\text{NO},\text{in}} \quad (18)$$

Integration of Eq. (17) and using the boundary condition (Eq. (18)) yields:

$$\frac{1}{k'_3} + \frac{1}{k'_3 K'_{\text{NO}}} \ln(C_{\text{NO},\text{in}}/C_{\text{NO},\text{out}}) = \frac{a_v L}{v_{\text{air}}(C_{\text{NO},\text{in}} - C_{\text{NO},\text{out}})} = \frac{BL}{Q(C_{\text{g},\text{in}} - C_{\text{g},\text{out}})} \quad (19)$$

with $Q = v_{\text{air}} BH$ and $C_{\text{NO},\text{out}} = C_{\text{NO}}(x=L)$. This equation was also obtained and successfully applied by Hunger et al. [28], who considered an NO balance only.

Thus employing Eqs. (16) and (19) plus the experimental data under different operating conditions, the kinetic parameters for the NO and NO₂ photocatalytic reaction can be obtained.

In Fig. 6, $y = BL/Q(C_{\text{NO},\text{in}} - C_{\text{NO},\text{out}})$ is set out vs. $x = \ln(C_{\text{NO},\text{in}}/C_{\text{NO},\text{out}})/(C_{\text{NO},\text{in}} - C_{\text{NO},\text{out}})$ (according to Eq. (19)), and the data fit with the line $y = (0.336 \text{ min dm}^{-1})x + 4.182 \times 10^7 \text{ min dm}^2 \text{ mol}^{-1}$. The intersection with the ordinate corresponds to $1/k'_3$, so that $k'_3 = 0.239 \times 10^{-7} \text{ mol dm}^{-2} \text{ min}^{-1}$, and the slope to $1/k'_3 K'_{\text{NO}}$, so that $K'_{\text{NO}} = 12.443 \times 10^7 \text{ dm}^3 \text{ mol}^{-1}$. The regression results are shown in Table 3 as well, including the standard errors and the 95% confidence intervals of the parameters. These values of $a_v k'_3$ and K'_{NO} are in line with those values k and K_d respectively presented by Hunger et al. [28].

At this time, from the NO kinetic parameters estimated with Eq. (19) and from Eq. (16), the kinetic information for the NO₂ photocatalytic reaction can be determined. Fig. 7 shows the NO₂ outlet concentration ($C_{\text{NO}_2,\text{out}}$) in function of NO outlet concentration ($C_{\text{NO},\text{out}}$) and the linear regression result with the ordinate intercept equal to zero. The slope obtained is $1/((k'_5 K'_{\text{NO}_2} / k'_3 K'_{\text{NO}}) - 1) = 0.084$ and therefore $k'_5 K'_{\text{NO}_2} = 38.41 \text{ dm min}^{-1}$ (Table 4). Considering Eq. (16), this result indicates that during the standard experiments the NO₂ at the outlet is about 8.4% of the NO

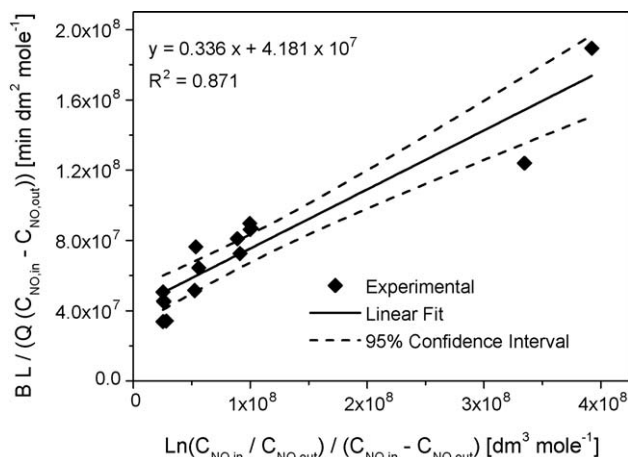


Fig. 6. Linear regression employing the approximate solution of the NO differential mass balance.

Table 3
Linear regression results employing the approximate solution of the NO differential mass balance.

Parameter	Value	Standard error	Lower 95% confidence interval	Upper 95% confidence interval
$\frac{1}{k_3 K_{NO}}$ (min dm ⁻¹)	0.336	0.034	0.262	0.410
$\frac{1}{k_5}$ (min dm ² mol ⁻¹)	4.18×10^7	0.51×10^7	3.09×10^7	5.27×10^7
k_3 (mol dm ⁻² min ⁻¹)	0.239×10^{-7}	0.029×10^{-7}	0.177×10^{-7}	0.302×10^{-7}
K'_{NO} (dm ³ mol ⁻¹)	12.44×10^7	2.76×10^7	6.46×10^7	18.43×10^7
R^2	0.871			
N (*)	15			

(*) Number of data.

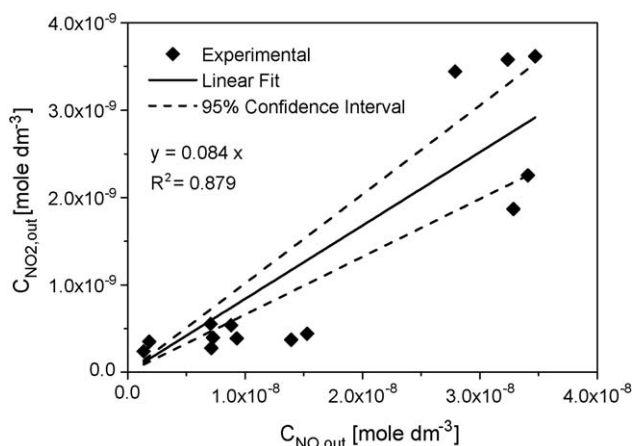


Fig. 7. Linear regression employing the approximate solution of the differential equation of NO₂ concentration in function of NO concentration.

concentration at the outlet, notwithstanding that NO₂ at the entrance is zero.

3.2. Complete solution

To solve the coupled NO and NO₂ mass balance with the complete kinetic expression, a discretization of the differential equations (Eqs. (11) and (12)) can be applied (Euler method):

$$v_{\text{air}} \frac{C_{\text{NO},i+1} - C_{\text{NO},i}}{x_{i+1} - x_i} = -a_v \frac{k_3 K_{\text{NO}} C_{\text{NO},i}}{1 + K_{\text{NO}} C_{\text{NO},i} + K_{\text{NO}_2} C_{\text{NO}_2,i}} \quad (20)$$

$$v_{\text{air}} \frac{C_{\text{NO}_2,i+1} - C_{\text{NO}_2,i}}{x_{i+1} - x_i} = a_v \left(-\frac{k_5 K_{\text{NO}_2} C_{\text{NO}_2,i}}{1 + K_{\text{NO}} C_{\text{NO},i} + K_{\text{NO}_2} C_{\text{NO}_2,i}} + \frac{k_3 K_{\text{NO}} C_{\text{NO},i}}{1 + K_{\text{NO}} C_{\text{NO},i} + K_{\text{NO}_2} C_{\text{NO}_2,i}} \right) \quad (21)$$

So

$$C_{\text{NO},i+1} = -a_v \left(\frac{k_3 K_{\text{NO}} C_{\text{NO},i}}{1 + K_{\text{NO}} C_{\text{NO},i} + K_{\text{NO}_2} C_{\text{NO}_2,i}} \right) \frac{x_{i+1} - x_i}{v_{\text{air}}} + C_{\text{NO},i} \quad (22)$$

Table 4
Linear regression results from the approximate solution of the differential equation of NO₂ concentration in function of NO concentration.

Parameter	Value	Standard error	Lower 95% confidence interval	Upper 95% confidence interval
$\frac{1}{(k_5 K_{\text{NO}_2} / k_3 K'_{\text{NO}})^{-1}}$	0.084	0.008	0.066	0.102
$\frac{k_5 K'_{\text{NO}_2}}{k_3 K'_{\text{NO}}}$	12.90	1.27	10.14	15.67
k_3 (mol dm ⁻² min ⁻¹)	0.239×10^{-7}	0.029×10^{-7}	0.177×10^{-7}	0.302×10^{-7}
K'_{NO} (dm ³ mol ⁻¹)	12.44×10^7	2.76×10^7	6.46×10^7	18.43×10^7
$k_5 K'_{\text{NO}_2}$ (dm min ⁻¹)	38.41	7.68	21.72	55.09
R^2	0.879			
N (*)	14			

(*) Number of data.

Table 5
Non-linear parameters optimization employing the Excel Solver tool and the numerical solution of the NO and NO₂ differential mass balance performing a forward discretization.

Parameter	Value	95% confidence interval
k_3 (mol dm ⁻² min ⁻¹)	0.47×10^{-7}	0.01×10^{-7}
K_{NO} (dm ³ mol ⁻¹)	3.40×10^7	0.08×10^7
k_5 (mol dm ⁻² min ⁻¹)	15.38×10^{-7}	0.02×10^{-7}
K_{NO_2} (dm ³ mol ⁻¹)	1.24×10^7	0.13×10^7
$k_5 K_{\text{NO}_2}$ (dm min ⁻¹)	19.07	2.10
$\frac{k_5 K_{\text{NO}_2}}{k_3 K_{\text{NO}}}$	11.93	1.71
N (*)	29	

$$C_{\text{NO}_2,i+1} = a_v \left(-\frac{k_5 K_{\text{NO}_2} C_{\text{NO}_2,i}}{1 + K_{\text{NO}} C_{\text{NO},i} + K_{\text{NO}_2} C_{\text{NO}_2,i}} + \frac{k_3 K_{\text{NO}} C_{\text{NO},i}}{1 + K_{\text{NO}} C_{\text{NO},i} + K_{\text{NO}_2} C_{\text{NO}_2,i}} \right) \frac{x_{i+1} - x_i}{v_{\text{air}}} + C_{\text{NO}_2,i} \quad (23)$$

where $i = 1 \dots N$ and $L_R = (x_{i+1} - x_i)(N - 1)$.

The optimum values of all kinetic parameters present in Eqs. (22) and (23) were obtained employing the Excel (Microsoft) “solver” tool. These results and the 95% confidence intervals are shown in Table 5. The estimated absorption constants for NO and NO₂ are in fairly agreement with those values calculated by Hashimoto et al. [8] employing titania-zeolite composite catalyst ($K_{\text{NO}} = 1.17 \times 10^7$ m³/mol and $K_{\text{NO}_2} = 0.44 \times 10^7$ m³/mol).

It is worth to mention that the values for the ratio ($k_5 K_{\text{NO}_2} / k_3 K_{\text{NO}}$) obtained in both approximate and complete models are nearly equal. In addition, the predicted ratio between the NO₂ and NO concentration at the reactor outlet by the complete model is approximately constant (NO₂ is about the (9.12 ± 0.17)% of NO at the reactor outlet) and this value is also in very good agreement with the ratio obtained in the approximate model. Nevertheless, it is important to notice that the values of $k_5 K_{\text{NO}_2}$ and $k_3 K_{\text{NO}}$ provided by both models differ by a factor of nearly two. This is certainly a consequence of the simplifications and parameters rearrangement made in the approximate model.

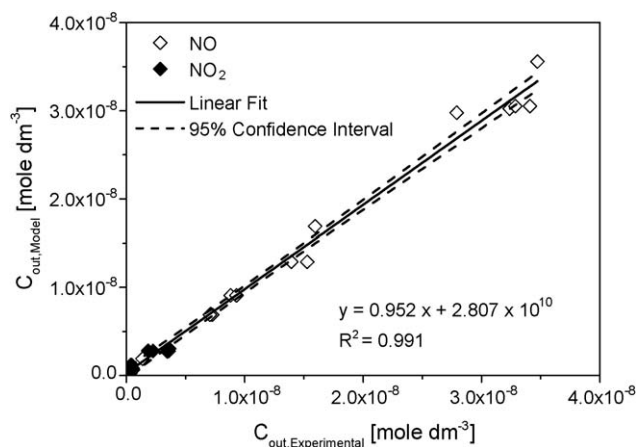


Fig. 8. NO and NO₂ outlet concentration predicted by the model employing the estimated kinetic parameters vs. the experimental data.

Fig. 8 shows the complete model predictions corresponding to the NO and NO₂ outlet concentration in function of the NO and NO₂ experimental data obtained in the photoreactor. These last values should be over a line with a slope close to 1 and an ordinate intercept equal to 0, as Fig. 8 and Table 6 show. In all cases, the model predictions show good agreement with the experimental results. Besides, the complete model predictions and the experimental values of the outlet concentration of NO and NO₂ can be compared in Table 7.

Despite of the accuracy and suitability of the complete model in predicting the experimental results, the approximate model can be easily and quickly applied to provide a rough but valuable estimation of the kinetic parameters involved. For instance, this

model could be very useful to practically evaluate the air purifying performance of photocatalytic construction materials using ISO 22197-1 standard [26].

4. Experimental results vs. modelling

It is possible to analyze the effect of different operating variables on the system by resorting the estimated kinetic parameters from the complete model. This analysis can include a comparison between simulated values obtained with the model and experimental measurements.

Fig. 9 shows the model predictions and the experimental data corresponding to the NO and NO₂ outlet concentration in function of the NO inlet concentration to the reactor for two different flow rates. When the inlet concentration of NO increases, both NO and NO₂ outlet concentration rise as well. However, as expected, decreasing the initial concentration of the pollutant the final conversion of the reacting system increases (see Table 1).

The effect of the flow rate is possible to analyze comparing Fig. 9(a) and (b). When the flow rate is increased the resident time in the reactor decreases. Therefore, for low flow rates a larger conversion of the pollutant is observed.

If the reactor height is varied, no changes in the outlet concentration are observed, as Fig. 10 shows for NO and NO₂ concentration. The explanation of this behavior can be found considering the height effect over the air velocity or resident time and over the total reactor volume. On the one hand, with higher reactor height lower air velocity and longer resident time are obtained resulting in a higher conversion. On the other hand, the reactor volume is larger and for the same photocatalytic active surface a smaller degradation conversion is achieved due to the products dissolution in the gas phase. These parameters (resident time and reactor volume) have opposite effects over the final conversion, resulting in a constant outlet concentration for different reactor heights.

Table 6

Linear regression results of the concentration predicted by the complete model vs. the experimental data.

Parameter	Value	Standard error	Lower 95% confidence interval	Upper 95% confidence interval
Slope	0.952	0.017	0.917	0.988
Ordinate intercept	2.81×10^{-10}	2.56×10^{-10}	-2.45×10^{-10}	8.06×10^{-10}
R ²	0.991			
N (*)	29			

(*) Number of data.

Table 7

Experimental and complete model results of the NO_x photocatalytic degradation.

Experiment #	C _{NO,in} × 10 ⁸ mol dm ⁻³	C _{NO,out} × 10 ⁸ mol dm ⁻³	C _{NO,out, Model} × 10 ⁸ mol dm ⁻³	C _{NO₂,in} × 10 ⁸ mol dm ⁻³	C _{NO₂,out} × 10 ⁸ mol dm ⁻³	C _{NO₂,out, Model} × 10 ⁸ mol dm ⁻³
1	0.430	0.136	0.190	0.008	0.024	0.018
2	1.357	0.712	0.696	0.015	0.028	0.064
3	1.346	0.725	0.690	0.016	0.040	0.064
4	1.346	0.705	0.690	0.024	0.055	0.064
5	2.257	1.392	1.290	0.019	0.037	0.119
6	2.257	1.527	1.290	0.039	0.044	0.119
7	4.419	2.789	2.978	0.066	0.344	0.272
8	4.472	3.237	3.023	0.081	0.358	0.276
9	4.506	3.287	3.052	0.072	0.187	0.278
10	4.507	3.410	3.052	0.063	0.225	0.278
11	0.454	0.184	0.281	0.010	0.035	0.026
12	1.342	0.882	0.910	0.020	0.054	0.083
13	1.342	0.930	0.911	0.023	0.039	0.083
14	2.242	1.594	1.690	–	–	0.150
15	4.458	3.472	3.558	0.087	0.362	0.306

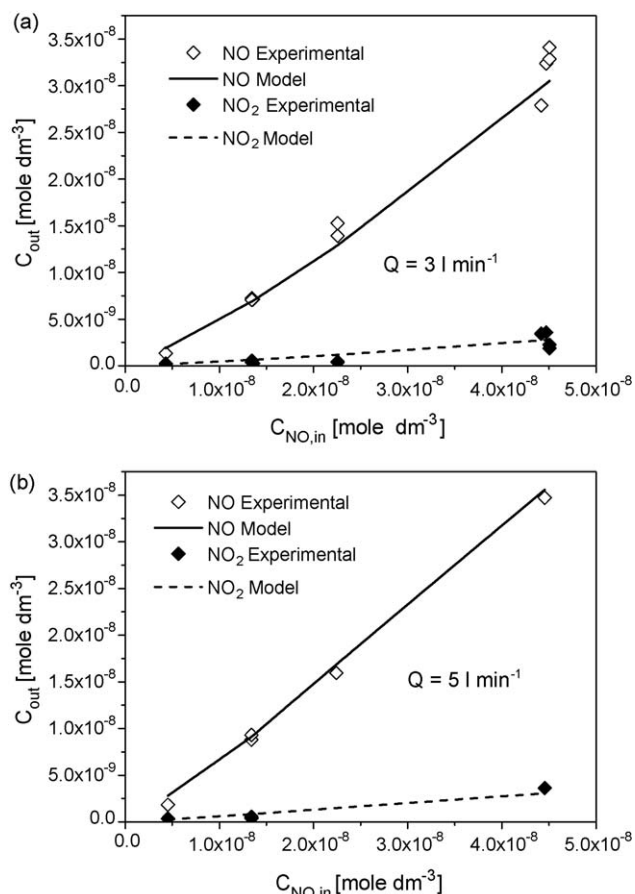


Fig. 9. Model predictions vs. experimental data. NO and NO₂ outlet concentration in function of the NO inlet concentration. (a) $Q = 3 \text{ l min}^{-1}$. (b) $Q = 5 \text{ l min}^{-1}$.

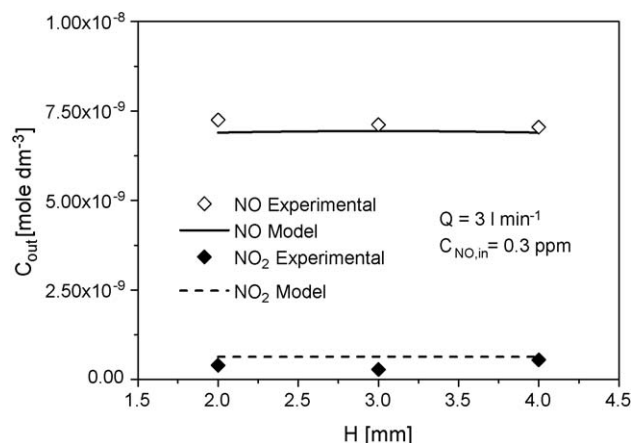


Fig. 10. Model predictions vs. experimental data. Effect of the reactor height over the degradation rate. $Q = 3 \text{ l min}^{-1}$. $C_{\text{NO},\text{in}} = 0.3 \text{ ppm}$.

5. Conclusion

In the present work, a kinetic study of the photocatalytic degradation of nitrogen oxides was conducted. A heterogeneous kinetic expression for the NO degradation and for the NO₂ appearance/disappearance was proposed. Several experiments were carried out according a suitable ISO standard for photocatalytic materials assessment employing only NO as the contaminant. Different operating conditions were selected to carry out the experiments (varying NO inlet concentration, reactor

height and flow rate) while relative humidity, temperature and irradiance remained constant during the experiments (50%, 20 °C and 10 W m^{-2}). Employing these experimental data and the kinetic expressions, the kinetic parameters for NO and NO₂ were estimated for an approximated and for a complete solution of the governing equations in the reactor and they were compared. In all cases, a very good correlation between the experimental data and the computer simulations with the estimated kinetic parameters was obtained, allowing to explain the degradation of NO and the apparition of NO₂ in this kind of system. A fixed NO₂/NO ratio of about 0.084–0.091 was found with both the approximate and the complete models.

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